

Drug Disposition Viewed in Terms of the Fractal Volume of Distribution

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Purpose. (i) Evaluate the predictive performance of the fractal volume of drug distribution, v_f (Pharm. Res.18, 1056, 2001), (ii) develop the concept of the fractal clearance, CL_f , which is the clearance analogue of v_f , (iii) examine the utility of CL_f in allometric studies, (iv) develop allometric relationships for the elimination half-life, $t_{1/2}$, and (v) evaluate the use of v_f and CL_f in predicting the volume of drug distribution, V_{ap} , clearance, CL , and elimination half-life, $t_{1/2}$.

Methods. Estimates for v_f of various drugs were obtained and correlated with body mass using data only from animal species. A comparison was made between the predicted and actual v_f values for humans. For a variety of animal species CL_f values were estimated from the equation:

$$CL_f = \frac{v_f}{V_{ap}} CL$$

The allometric equations developed using CL_f were compared with other allometric approaches. Allometric equations were also developed for $t_{1/2}$ utilizing the allometric relationships of v_f and CL_f .

Results. The predicted estimates of v_f were very close to the actual values and the correlation exhibited favorable statistical properties. The values of the allometric exponents for CL_f were found to be close to 0.75. The predictive performance for CL using the allometric equations for CL_f in conjunction with the rule of exponents was found to be better than the currently considered most accurate allometric approaches. The values of the allometric exponents for $t_{1/2}$ were found to be close to 0.25.

Conclusion. The predictive ability of v_f is high; predictions for V_{ap} based on v_f values are better than the current approaches. CL_f expressed a good behavior both in prospective and retrospective analysis. The allometric exponents, 0.75, 0.25 for CL_f and $t_{1/2}$, respectively, agree with the theoretical expected values.

KEY WORDS: allometry; clearance; volume of distribution; elimination half-life; fractal.

INTRODUCTION

The concept of clearance originates from the physiological function of the eliminating organs (1). In this respect, organ clearance is highly associated with the organ blood flow, is expressed in units of flow rate while the specific organ blood flow comprises a physiological maximum for the measured clearance, e.g., hepatic clearance ≤ 1350 mL/min (1). Based on the additive properties of clearance, the concept of body clearance, CL , which expresses globally the ability of the eliminating organs of the body to remove drug is being used extensively in pharmacokinetics (1). Estimates for CL can be derived from Eq. (1), which indicates that CL is a proportionality constant between the dose reaching the general circulation and the measured area under the plasma drug concentration-time curve, (AUC):

$$Dose = CL(AUC) \quad (1)$$

While CL can be used to characterize drug elimination, the distribution of drug in the body can be characterized by the volume of drug distribution, V_{ap} . The values of the two primary pharmacokinetic parameters, CL and V_{ap} , determine the values of the secondary pharmacokinetic parameters, elimination rate constant, k , and elimination half-life, $t_{1/2}$:

$$k = \frac{\ln 2}{t_{1/2}} = \frac{CL}{V_{ap}} \quad (2)$$

Equation (2) indicates that k and $t_{1/2}$ reflect the values of CL and V_{ap} but not *vice versa* (2). According to Eq. (2), CL refers to the portion of V_{ap} that is cleared per unit of time.

Recently, we developed the physiologically sound concept of fractal volume of drug distribution, v_f (3). This novel parameter takes values smaller or equal to the body mass (expressed in volume units) of the species and corresponds to the part of the total volume of the species body in which the drug is distributed at equilibrium. Using allometric principles, it was found that v_f scales proportionally to body mass (3).

In this study, we first investigate the use of v_f in prospective studies. Further, we examine the properties of the clearance analogue of v_f , called for reasons of uniformity fractal clearance, CL_f ; the latter refers to the portion of v_f cleared per unit of time. This quest is justified by the fact that the concepts of volume of distribution and clearance are always linked via the secondary pharmacokinetic parameter $t_{1/2}$ or k [Eq. (2)]. To this end, we calculated the values of CL_f for various drugs utilizing the reported v_f values (3) keeping unaltered the reported elimination rate constant or half-life. Moreover, we applied allometric analysis to the calculated CL_f values of various drugs in different species and compared our results with the allometric studies for clearance reported in the literature. Also, allometric equations for $t_{1/2}$ were derived from allometric relationships of CL_f and v_f . Finally, the use of v_f and CL_f in predicting V_{ap} , CL , and $t_{1/2}$ was evaluated.

METHODS

Values of V_{ap} for several drugs were transformed to their v_f analogs, using Eq. (3) reported previously (3):

$$v_f = V_{pl} + (v - V_{pl}) \frac{V_{ap} - V_{pl}}{V_{ap}} \quad (3)$$

where v is the total volume of the species (equivalent to its total mass assuming a uniform density 1g/mL), V_{pl} is the plasma volume of the species and V_{ap} is the conventional volume of drug distribution. Allometric equations were generated, utilizing the v_f estimates for various drugs in different species. To evaluate the usefulness of v_f in prospective studies, i.e., in studies where prediction of the human v_f value from animal data is attempted, human data were not included in the allometric analysis.

Also, predictions for V_{ap} using v_f were based on Eq. (4) which is derived from Eq. (3):

$$V_{ap} = V_{pl} \frac{(v - V_{pl})}{(v - v_f)} \quad (4)$$

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Based on the conceptual meaning of CL_f and v_f i.e., CL_f denotes the portion of v_f which is cleared per unit of time, one can write:

$$k = \frac{\ln 2}{t_{1/2}} = \frac{CL_f}{v_f} \quad (5)$$

Equations (2) and (5) ensure that the value of the observable parameter k or $t_{1/2}$ remains unaltered whether classical (CL , V_{ap}) or fractal (CL_f , v_f) disposition is considered. Eq. (6) is obtained by dividing Eqs.(2) and (5):

$$CL_f = \frac{v_f}{V_{ap}} CL \quad (6)$$

The available in literature CL values for various drugs were transformed to the corresponding CL_f values using Eq. (6). The estimates for CL_f were subjected to allometric analysis. For comparative purposes, allometric analysis of the same data was also performed using the conventional clearance, CL , and the composite parameters $CL \cdot MLP$ (4) and $CL \cdot BW$ (5), where MLP and BW refer to maximum lifespan potential and brain weight, respectively. Also, predictions for CL were derived from Eq. (6) using V_{ap} values obtained from Eq. (4).

In all cases success was assessed by the geometric mean of the logarithmic ratio of predicted and actual values (6) of N drugs:

$$\text{Average-Fold Relative Error} = 10^{\frac{\left| \sum \log \frac{\text{Predicted}}{\text{Actual}} \right|}{N}} \quad (7)$$

The ideal value of average-fold relative error, AFRE, is 1, which means that the method predicts all actual values perfectly. The prediction becomes less precise as the deviation of AFRE from unity becomes larger. Besides, the average relative error (%ARE), which corresponds to $100(\text{predicted-actual})/\text{actual}$, was used to evaluate the predictions (6).

RESULTS

Although in our previous study (3) we found very good linear correlations between the logarithms of v_f and the body mass of the species, in this work we further wanted to investigate whether the successive correlation implies also an accurate precision for v_f (7,8). For each one of the species (except man) the value of v_f was derived from Eq. (3) using the reported in literature V_{ap} values. The calculated v_f values were further used to develop allometric equations. Then, the human mass value reported in the relevant article was used to derive from these equations the predicted estimates for human v_f . The expected values of v_f were obtained from Eq. (3) using the apparent volume of drug distribution for humans reported in the reference article. Fig. 1 shows the relationship between the predicted and the expected v_f values. Visual inspection of Fig. 1, illustrates not only a good linear relationship between the predicted and observed values of v_f but also the almost ideal concordance (slope = 0.96). Moreover, evaluation of the predictive performance of v_f with the geometric mean of the ratio of predicted and actual values utilizing Eq. (7) gave AFRE and %ARE values equal to 1.04 and 4.04%, respectively. It is interesting to note that the allometric equations for the conventional V_{ap} using the same data gave AFRE and %ARE values 1.72, 146.8%, respec-

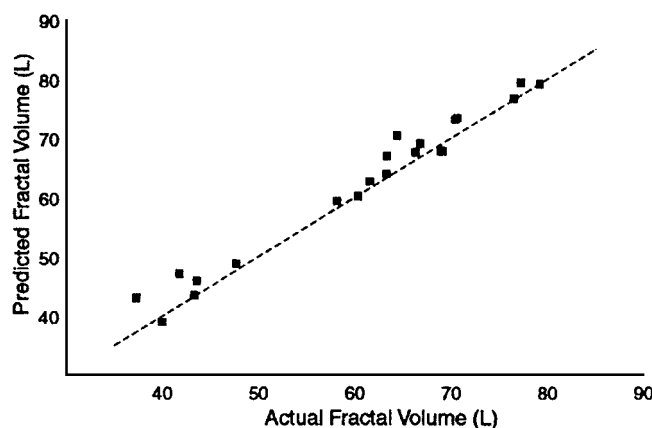


Fig. 1. Plot of predicted from allometric scaling human values of v_f (ordinate) vs. actual human v_f values (abscissa). Actual v_f values were derived from Eq. (3) using the human V_{ap} values quoted in the literature (13-28). The dashed line indicates complete concordance.

tively. In addition, the literature values for AFRE, utilizing various scaling approaches for the prediction of the apparent volume of drug distribution, have been found (6) much higher, e.g., 1.56, 1.56, 1.83, 2.78; also, the AFRE value for the scaling of the volume of distribution of the central compartment was found 1.3 (9). This means that one can derive an accurate estimate for v_f in humans using data only from animal species.

Because V_{ap} can be used to determine the initial concentration of drug after an i.v. administration for the selection of the first time dose in humans (10), we calculated V_{ap} values using v_f . For each one of the species (except human) the value of V_{ap} was derived from Eq. (4) using the corresponding v_f values. The V_{ap} values were used to develop allometric equations which were further used to predict human V_{ap} estimates. The AFRE and %ARE for the predicted V_{ap} values were 1.51 and 99.2%, respectively. These indexes are much better than the aforementioned values 1.72 and 146.8% for V_{ap} derived conventionally. This means that one can derive a more reliable estimate for V_{ap} using v_f than the current approaches and since the administrated dose is known it can be used to calculate plasma concentration at time zero.

The results of the allometric analysis for clearance using four approaches are listed in Table I. The four approaches compared are based on the values of CL_f , CL , $CL \cdot MLP$ and $CL \cdot BW$. Although the use of MLP and BW may not have any physiological meaning, it has been suggested that both parameters help in improving the predictive performance in scaling (10). Estimates for MLP and BW were taken either from the relevant article or were calculated using the body and brain weights (11) of the species as described in the literature (12). For comparative purposes, all data were expressed to identical units; thus, the kilogram was used as the measure of mass and L/h as the unit of clearance. The symbols CL_{tot} , CL_{ren} and CL_{hep} characterize the type of clearance, i.e., total, renal and hepatic clearance, respectively. The values of CL_{ren} and CL_{hep} were either quoted in literature or calculated from the reported data (13-28). Visual inspection of Table I reveals that the allometric equations of CL_f exhibit coefficient of determination values (R^2) higher than CL and comparable with the best values of $CL \cdot MLP$ and $CL \cdot BW$. Moreover, the allometric exponents of CL_f never exceeded

Table I. Allometric Equations Describing the Relationship between the Various Types of Clearance and Body Mass across Species

Drug ^a	CL _f	R ²	CL	R ²	CL · MLP	R ²	CL · BW	R ²
Actisomide (V _d)	(CL _{tot}) _f = 0.526 M ^{0.948}	0.995	CL _{total} = 0.641 M ^{0.951}	0.973	CL _{tot} · MLP = 0.0503 10 ⁶ M ^{1.485}	0.979	CL _{tot} · BW = 0.0053 M ^{2.158}	0.987
	(CL _{ren}) _f = 0.201 M ^{0.898}	0.998	CL _{renal} = 0.2445 M ^{0.901}	0.991	CL _{ren} · MLP = 0.0192 10 ⁶ M ^{1.435}	0.992	CL _{ren} · BW = 0.0020 M ^{2.108}	0.994
	(CL _{hep}) _f = 0.157 M ^{0.986}	0.893	CL _{hep} = 0.191 M ^{0.990}	0.936	CL _{hep} · MLP = 0.0150 10 ⁵ M ^{1.523}	0.983	CL _{hep} · BW = 0.00158 M ^{2.196}	0.993
Amphotericin (V ₁)	CL _f = 0.052 M ^{0.886}	0.950	CL = 0.0559 M ^{0.827}	0.946	CL · MLP = 5.703 10 ³ M ^{1.242}	0.988	CL · BW = 0.000719 M ^{1.827}	0.996
Amphotericin (V _{ap})	CL _f = 0.020 M ^{0.867}	0.974	CL = 0.0559 M ^{0.827}	0.940	CL · MLP = 5.703 10 ³ M ^{1.242}	0.988	CL · BW = 0.000719 M ^{1.827}	0.996
Amphotericin (V _{ss})	CL _f = 0.0195 M ^{0.849}	0.965	CL = 0.0559 M ^{0.827}	0.940	CL · MLP = 5.703 10 ³ M ^{1.242}	0.988	CL · BW = 0.000719 M ^{1.827}	0.996
Amsacrine (V _{ss})	CL _f = 0.670 M ^{0.646}	0.987	CL = 2.29 M ^{0.460}	0.906	CL · MLP = 1.91 10 ⁵ M ^{0.856}	0.921	CL · BW = 0.020 M ^{1.433}	0.947
BSH (V _{ap})	CL _f = 0.08 M ^{0.807}	0.964	CL = 0.128 M ^{0.676}	0.946	CL · MLP = 1.16 10 ⁴ M ^{1.133}	0.997	CL · BW = 0.00136 M ^{1.772}	0.999
Cefazolin (V _{ss})	(CL _{tot}) _f = 1.146 M ^{0.714}	0.992	CL _{tot} = 0.271 M ^{0.680}	0.975	CL _{tot} · MLP = 0.0236 10 ⁶ M ^{1.126}	0.996	CL _{tot} · BW = 0.00257 M ^{1.752}	0.997
	(CL _{ren}) _f = 0.873 M ^{0.781}	0.981	CL _{ren} = 0.206 M ^{0.746}	0.965	CL _{ren} · MLP = 0.0179 10 ⁶ M ^{1.192}	0.997	CL _{ren} · BW = 0.00196 M ^{1.819}	0.998
Cefmetazole (V _{ss})	(CL _{tot}) _f = 2.25 M ^{0.711}	0.972	CL _{tot} = 0.736 M ^{0.594}	0.917	CL · MLP = 0.1148 10 ⁶ M ^{0.771}	0.947	CL _{tot} · BW = 0.0123 M ^{1.396}	0.970
	(CL _{ren}) _f = 1.268 M ^{0.784}	0.965	CL _{ren} = 0.415 M ^{0.668}	0.959	CL · MLP = 0.036 10 ⁶ M ^{1.108}	0.990	CL _{ren} · BW = 0.00389 M ^{1.733}	0.991
Cefoperazone (V _{ss})	(CL _{tot}) _f = 1.403 M ^{0.634}	0.908	CL _{tot} = 0.402 M ^{0.571}	0.823	CL _{tot} · MLP = 0.0377 10 ⁶ M ^{0.988}	0.959	CL _{tot} · BW = 0.0045 M ^{1.580}	0.983
	(CL _{ren}) _f = 0.465 M ^{0.699}	0.838	CL _{ren} = 0.133 M ^{0.635}	0.704	CL _{ren} · MLP = 0.01023 10 ⁵ M ^{1.144}	0.944	CL _{ren} · BW = 0.00112 M ^{1.784}	0.985
Cefotetan (V _{ss})	(CL _{tot}) _f = 1.396 M ^{0.576}	0.917	CL _{tot} = 0.379 M ^{0.533}	0.849	CL _{tot} · MLP = 0.0337 10 ⁶ M ^{0.972}	0.990	CL _{tot} · BW = 0.00367 M ^{1.596}	0.999
	(CL _{ren}) _f = 0.872 M ^{0.589}	0.923	CL _{ren} = 0.237 M ^{0.547}	0.865	CL _{ren} · MLP = 0.021 10 ⁶ M ^{0.986}	0.989	CL _{ren} · BW = 0.0023 N ^{1.609}	0.997
Cefpiramide (V _{ss})	(CL _{tot}) _f = 0.769 M ^{0.542}	0.890	CL _{tot} = 0.245 M ^{0.404}	0.589	CL _{tot} · MLP = 0.022 10 ⁶ M ^{0.842}	0.875	CL _{tot} · BW = 0.0025 M ^{1.461}	0.953
	(CL _{ren}) _f = 0.328 M ^{0.567}	0.791	CL _{ren} = 0.105 M ^{0.429}	0.522	CL · MLP = 0.093 10 ⁵ M ^{0.867}	0.860	CL _{ren} · BW = 0.00105 M ^{1.486}	0.954
CI-921 (V _{ss})	CL _f = 0.707 M ^{0.815}	0.943	CL = 0.914 M ^{0.507}	0.830	CL · MLP = 7.32 10 ⁴ M ^{0.913}	0.910	CL · BW = 0.007 M ^{1.503}	0.944
Diazepam (V ₁)	CL _f = 2.78 M ^{0.459}	0.605	CL = 7.29 M ^{0.103}	0.037	CL · MLP = 0.436 10 ⁶ M ^{0.604}	0.721	CL · BW = 0.0367 M ^{1.234}	0.902
Diazepam (V _β)	CL _f = 0.885 M ^{0.353}	0.879	CL = 7.29 M ^{0.103}	0.037	CL · MLP = 0.436 10 ⁶ M ^{0.604}	0.721	CL · BW = 0.0367 M ^{1.234}	0.902
Diazepam (V _{ss})	CL _f = 1.451 M ^{0.315}	0.628	CL = 7.29 M ^{0.103}	0.037	CL · MLP = 0.436 10 ⁶ M ^{0.604}	0.721	CL · BW = 0.0367 M ^{1.234}	0.902
Erythromycin (V _{ss})	CL _f = 0.591 M ^{0.886}	0.985	CL = 2.32 M ^{0.713}	0.963	CL · MLP = 0.201 10 ⁶ M ^{1.119}	0.999	CL · BW = 0.0228 M ^{1.705}	0.998
Interferon-a (V _{ss})	CL _f = 0.872 N ^{0.750}	0.961	CL = 0.221 M ^{0.710}	0.980	CL · MLP = 0.0185 10 ⁶ M ^{1.094}	0.969	CL · BW = 0.002 M ^{1.685}	0.975
Lamifiban (V _{ss})	CL _f = 1.085 M ^{0.632}	0.919	CL = 0.368 M ^{0.884}	0.887	CL · MLP = 0.03167 10 ⁶ M ^{1.311}	0.997	CL · BW = 0.00367 M ^{1.891}	0.995
Moxalactame (V _{ss})	(CL _{tot}) _f = 1.118 M ^{0.718}	0.996	CL _{tot} = 0.302 M ^{0.662}	0.992	CL _{tot} · MLP = 0.0262 10 ⁶ M ^{1.107}	0.993	CL _{tot} · BW = 0.0029 M ^{1.732}	0.993
	(CL _{ren}) _f = 0.889 M ^{0.769}	0.990	CL _{ren} = 0.240 M ^{0.713}	0.981	CL _{ren} · MLP = 0.0209 10 ⁶ M ^{1.159}	0.995	CL _{ren} · BW = 0.0023 M ^{1.783}	0.994
Oleandomycin (V _{ss})	CL _f = 0.656 M ^{0.934}	0.990	CL = 1.828 M ^{0.691}	0.995	CL · MLP = 0.0178 10 ⁷ M ^{1.108}	0.991	CL · BW = 0.0218 M ^{1.700}	0.992
Phencyclidine (V _β)	CL _f = 0.314 M ^{0.675}	0.953	CL = 3.617 M ^{0.616}	0.907	CL · MLP = 0.032 10 ⁷ M ^{1.035}	0.991	CL · BW = 0.03967 M ^{1.624}	0.995
Procaterol (V _β)	(CL _{tot}) _f = 0.61 M ^{0.768}	0.992	CL _{tot} = 1.74 M ^{0.827}	0.991	CL _{tot} · MLP = 1.22 10 ⁵ M ^{1.192}	1.000	CL _{tot} · BW = 0.013 M ^{1.712}	0.998
	(CL _{ren}) _f = 0.14 M ^{0.897}	0.993	CL _{ren} = 0.4 M ^{0.956}	0.994	CL _{ren} · MLP = 2.81 10 ⁴ M ^{1.321}	1.000	CL _{ren} · BW = 0.003 M ^{1.841}	0.998
	(CL _{hep}) _f = 0.46 M ^{0.727}	0.992	CL _{hep} = 1.32 M ^{0.786}	0.989	CL _{hep} · MLP = 9.3 10 ⁴ M ^{1.151}	1.000	CL _{hep} · BW = 0.0097 M ^{1.671}	0.998
Procaterol (V _c)	(CL _{tot}) _f = 2.88 M ^{0.863}	0.999	CL _{tot} = 1.74 M ^{0.827}	0.991	CL _{tot} · MLP = 1.22 10 ⁵ M ^{1.192}	1.000	CL _{tot} · BW = 0.013 M ^{1.712}	0.998
	CL _{ren}) _f = 0.66 M ^{0.991}	0.999	CL _{ren} = 0.4 M ^{0.956}	0.994	CL _{ren} · MLP = 2.81 10 ⁴ M ^{1.321}	1.000	CL _{ren} · BW = 0.003 M ^{1.841}	0.998
	(CL _{hep}) _f = 2.19 M ^{0.822}	0.999	CL _{hep} = 1.32 M ^{0.786}	0.989	CL _{hep} · MLP = 9.3 10 ⁴ M ^{1.151}	1.000	CL _{hep} · BW = 0.0097 M ^{1.671}	0.998
Remoxipride (V _{ss})	(CL _{tot}) _f = 0.925 M ^{0.525}	0.978	CL _{tot} = 2.1 M ^{0.335}	0.854	CL _{tot} · MLP = 0.0188 10 ⁷ M ^{0.745}	0.976	CL _{tot} · BW = 0.0203 M ^{1.328}	0.987
	(CL _{ren}) _f = 0.130 M ^{0.631}	0.964	CL _{ren} = 0.298 M ^{0.441}	0.926	CL _{ren} · MLP = 0.0265 10 ⁶ M ^{0.851}	0.969	CL _{ren} · BW = 0.00283 M ^{1.434}	0.980
Tamsulosin (V _d)	CL _f = 1.422 M ^{0.677}	0.999	CL _{tot} = 3.67 M ^{0.594}	0.993	CL _{tot} · MLP = 0.0242 10 ⁷ M ^{0.878}	0.994	CL · BW = 0.0275 M ^{1.383}	0.993
Theophylline (V _{ss})	(CL _{hep}) _f = 0.275 M ^{0.729}	0.999	CL _{hep} = 0.161 M ^{0.784}	0.965	CL _{hep} · MLP = 0.098 10 ⁵ M ^{1.325}	0.998	CL _{hep} · BW = 0.00105 M ^{1.992}	0.999
	(CL _{intr}) _f = 0.602 M ^{0.660}	0.998	CL _{intr} = 0.353 M ^{0.715}	0.975	CL _{intr} · MLP = 0.0215 10 ⁶ M ^{1.256}	1.000	CL _{intr} · BW = 0.0023 M ^{1.923}	0.998
Troglitazone (V _β)	CL _f = 0.38 M ^{0.723}	0.994	CL = 0.742 M ^{0.808}	0.988	CL · MLP = 0.0648 10 ⁶ M ^{1.198}	0.994	CL · BW = 0.007 M ^{1.781}	0.996
Troglitazone (V _c)	CL _f = 2.02 M ^{0.808}	0.991	CL = 0.742 M ^{0.808}	0.988	CL · MLP = 0.0648 10 ⁶ M ^{1.198}	0.994	CL · BW = 0.007 M ^{1.781}	0.996
Troglitazone (V _{ss})	CL _f = 0.820 M ^{0.826}	0.996	CL = 0.742 M ^{0.808}	0.988	CL · MLP = 0.0648 10 ⁶ M ^{1.198}	0.994	CL · BW = 0.007 M ^{1.781}	0.996

^a The volume term in parenthesis was used for the calculation of v_f from Eq. 3.

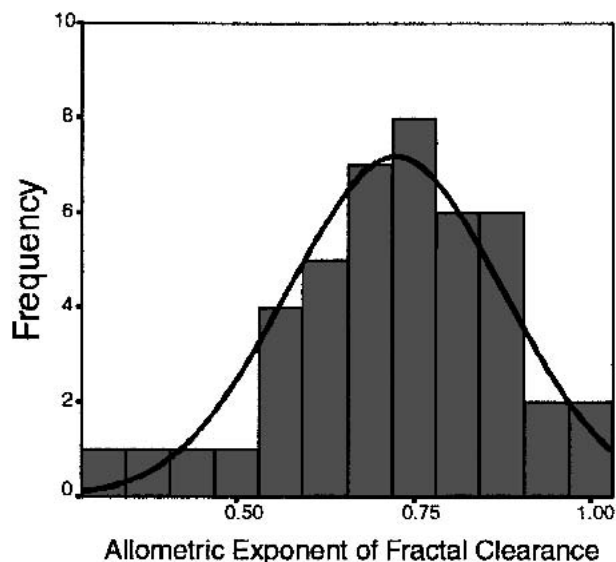


Fig. 2. Histogram for the allometric mass exponent of CL_f listed in Table I.

unity, which is frequently the case for the allometric equations of $CL \cdot MLP$ and $CL \cdot BW$. In some cases, the equations for $CL \cdot BW$ had exponents very close to 2. The smaller than unity values found for the allometric exponents of CL_f are in accord with the theoretical expectations, which suggest that smaller organisms have a greater opportunity to dispose drug molecules. Figure 2 shows the distribution of the numerical values of the allometric exponents for CL_f . The graph of Fig. 2 reveals that the values of the exponents are normally distributed around the mean value 0.72 (median 0.73, and CV $\sim 3.2\%$), which is very close to the expected value 0.75. A characteristic example is interferon- α which exhibits ideal behavior (Table I, allometric exponent 0.750). According to Lavé *et al.* (21), who found 0.71 for the allometric exponent of interferon- α clearance, the scaling works best for interferon- α since it is mainly eliminated by physical transport processes. Their conclusions for interferon- α are verified in our study using CL_f as clearance parameter. Overall, the homogeneous normal distribution of the allometric exponents for CL_f indicates that CL_f scales as a $3/4$ power of mass i.e., $CL_f \propto M^{3/4}$. This finding is in accord with the general scaling law for clearance, the origin of which was recently found to be associated

Table II. Predicted and Observed Human Values of Fractal Clearance and Conventional Clearance

Drug	Fractal clearance (L/h)			Clearance (L/h)			
	Predicted		Observed ^a	Predicted from			Observed
	CL_f	$(CL_f)_e$		CL_f^b	$(CL_f)_e^b$	CL_e	
Actisomide (CL_{tot})	32.75	22.60	23.72	34.51	23.82	35.34	25.44
Actisomide (CL_{ren})	9.1	7.34	7.83	9.59	7.74	11.48	8.4
Actisomide (CL_{met})	19.44	13.42	13.52	20.48	14.14	20.98	14.5
Amphotericin (CL_{tot})	1.23	0.72	1.54	1.14	0.67	1.15	1.8
Amsacrine (CL_{tot})	9.73	9.73	13.19	15.71	15.71	13.74	21.14
BSH (CL_{tot})	11.22	2.59	1.62	13.32	3.08	3.22	1.51
Cefazolin (CL_{tot})	24.62	12.68	18.32	5.03	2.59	3	3.18
Cefazolin (CL_{ren})	27.85	14.34	16.67	5.69	2.93	3.24	2.89
Cefmetazole (CL_{tot})	50.67	24.89	33.42	10.26	5.04	10.35	6.7
Cefmetazole (CL_{ren})	35.32	17.35	28.07	7.15	3.51	7.21	5.63
Cefoperazone (CL_{tot})	19.39	19.39	21.07	4.08	4.08	4.6	4.24
Cefoperazone (CL_{ren})	19.87	12.72	5.27	4.18	2.68	3.18	1.06
Cefotetan (CL_{tot})	22.16	22.16	9.42	5.32	5.32	5.87	1.81
Cefotetan (CL_{ren})	12.78	12.78	7.25	3.07	3.07	3.38	1.4
Cefpiramide (CL_{tot})	8.71	8.71	5.98	1.51	1.51	1.61	1.05
Cefpiramide (CL_{ren})	7.32	3.80	1.49	1.27	0.66	1.36	0.26
CI-921 (CL_{tot})	16.27	5.24	30.73	6.84	2.20	5.33	11.28
Diazepam (CL_{tot})	33.32	16.62	4.55	70.74	54.79	84.91	2.84
Erythromycin (CL_{tot})	21.47	7.80	31.79	70.75	25.70	31.19	29.52
Moxalactame (CL_{tot})	18.89	18.89	25.19	4.03	4.03	4.37	4.95
Moxalactame (CL_{ren})	19.35	10.07	23.68	4.13	2.15	2.32	4.65
Oleandomycin (CL_{tot})	22.6	9.86	46.91	28.4	12.38	28.85	38.22
Phencyclidine (CL_{tot})	9.71	5.57	3.63	105.24	60.34	72.26	22.64
Remoxipride (CL_{tot})	6.93	6.93	11.25	9.29	9.29	10.86	8.36
Remoxipride (CL_{ren})	1.02	1.03	3.31	1.37	1.37	1.6	2.46
Theophylline (CL_{intr})	8.01	8.01	9.95	6.35	6.35	4.84	5.78
Theophylline (CL_{met})	5.62	2.79	5.63	4.46	2.21	3.4	3.27
Statistical indexes							
AFRE	1.31	1.21		1.65	1.06	1.42	
%ARE	82.8	8.43		181.3	84.66	157.8	

^a Calculated from Eq. 6 using the reported values for V_{ap} and CL ; v_f was obtained from Eq. 3.

^b The predicted values for clearance were derived from Eq. 6 which was solved in terms of CL ; V_{ap} estimates were obtained from Eq. 4 using predicted human v_f values.

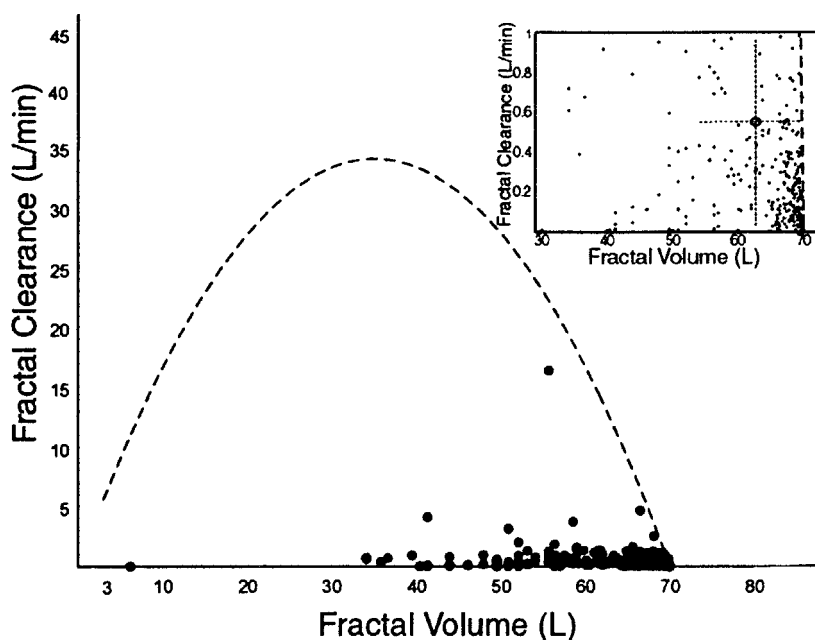


Fig. 3. Plot of CL_f vs. v_f using Eq. (8) for humans assigning $V_{pl}=3L$, $v=70L$, and $CL=5.6$ L/min (cardiac output). The values of v_f , CL_f of the data points plotted were calculated from Eqs. (3) and (6), respectively, utilizing V_{ap} and CL values taken from the literature (32). A total of 309 drugs are plotted. The inset magnifies the region 0–1 L/min of the ordinate. The symbol (ϵ) indicates the cutoff point 63 L, 0.56 L/min.

with the fractal like architecture of the interior networks that distribute resources within organisms (29,30).

Because a good correlation does not surely imply a good prediction (7,8), the usefulness of CL_f in prospective studies was also explored. To this end, data from various animal species, except human, were used to calculate the allometric equations based on the CL_f values. For comparative reasons the same calculations were used for the estimation of the allometric equations with conventional clearance, CL , and its composites with MLP and BW applying the “rule of exponents” (31). The rule of exponents is empirically based on the exponent values of the simple allometry and it was proposed (31) to specify under what conditions the allometric equation, involving either CL , $CL \cdot MLP$, or $CL \cdot BW$ can be used for more accurate prediction of clearance. Table II shows the predicted clearance values with various approaches; the term CL_e quoted in Table II denotes classical clearance derived from the rule of exponents. Comparing the results for CL_f and those derived from the approaches that are currently proposed to be most accurate, it can be concluded that CL_f exhibits better predictive performance than CL_e since the values of AFRE and %ARE are 1.31, 82.8% and 1.42, 157.8%, respectively (Table II). Furthermore, when CL_f is used in conjunction with the rule of exponents (the so derived fractal clearance is denoted with $(CL_f)_e$) the statistical indexes exhibit even better performance i.e., 1.21 and 8.43%.

For practical purposes, the conventional clearance, CL , was calculated from Eq. (6) using CL_f values. Besides, the same calculations were performed for CL using $(CL_f)_e$ values. The results demonstrate that the best predictive performance (AFRE: 1.06, %ARE: 84.66%) is obtained when CL is derived from $(CL_f)_e$. Overall, the predictive performance of the various clearance expressions for the conventional CL follows the ranking: $(CL_f)_e > CL_e > CL_f$, Table II. One should note

however that clearance, CL , derived from CL_f requires only one transformation applicable to all cases and it does not rely on any empirical assumption (7,8). On the contrary, the approaches utilizing the rule of exponents are more complicated, use empirical correction parameters (BW , MLP), while the selection of the exponent is empirical too.

Drug clearance values are better understood when considered in the light of the upper limit values imposed by the physiology. Such a consideration for CL_f can be based on Eq. (8) derived from Eqs. (4) and (6):

$$CL_f = \frac{v_f(v - v_f)}{V_{pl}(v - V_{pl})} CL \quad (8)$$

Equation (8) reveals that CL_f can be higher or lower than CL depending on the value of v_f , i.e., $CL_f > CL$ when $3L < v_f < 67L$ and $CL_f < CL$ when $70L > v_f > 67L$. The two terms, CL , and CL_f become identical when the drug is confined to plasma, i.e., $v_f = V_{pl} = 3L$. Besides, Eq. (8) allows us to calculate the range of the physiologically permitted CL_f values in various species. The results obtained for humans by assigning $v = 70$ L, $V_{pl} = 3$ L and $CL = 5.6$ L/min which is the physiological maximum for the cardiac output (11), are presented in Fig. 3. The physiologically acceptable values for the pairs v_f , CL_f lie in the area under the curve of Fig. 3. Accordingly, a large number of drugs taken from the literature (32) were found to lie in this area exclusively. The boundaries imposed by the physiology for CL_f and v_f (3) in conjunction with their functional relationship [Eq. (8)] can be used to develop a pharmacokinetic drug classification scheme (PCS), Fig. 3. The PCS attempts to bring the space-time considerations in pharmacokinetics (33) in a real physiological context. This can be achieved by selecting a cutoff point for both pharmacokinetic parameters [“volume of distribution” for space and “clear-

Table III. Drug Examples Classified into Four Categories of PCS Using the Cutoff Point 63 L, 0.56 L/min in the v_f , CL_f Plane

Class I (HH) ^a $v_f > 63$ L, $CL_f > 0.56$ L/min	Erythromycin, Zidovudine, Haloperidol, Ketamine, Minoxidil
Class II (LH) ^a $v_f \leq 63$ L, $CL_f > 0.56$ L/min	Acetylsalicylic acid, Cefaclor, Chlorothiazide, Cloxacillin, Dicloxacillin
Class III (LL) ^a $v_f \leq 63$ L, $CL_f \leq 0.56$ L/min	Glipizide, Ibuprofen, Indomethacin, Ketoprofen, Phenobarbital
Class IV (HL) ^a $v_f > 63$ L, $CL_f \leq 0.56$ L/min	Diazepam, Fentanyl, Amiodarone, Caffeine, Chloramphenicol

^a H denotes high; L denotes low.

ance" for time, (33)] on the basis of physiological considerations. However, the way we conceive the distribution of drug in the body (space, fractal volume) is of primary importance and crucial for the temporal element (fractal clearance) as the concept of clearance refers to the volume cleared per time unit and therefore is by definition dependent on the notion of volume. Consequently, the value of 63 L was assigned first for the cutoff point of v_f since it corresponds to the 90% of the physiological maximum (70 L) and is very close to the mean value (63.6 L) of v_f for the 309 data analyzed (32). The most plausible physiological maximum for the corresponding temporal component of our classification is the total cardiac output 5.6 L/min. This value when combined with the physiological maximum for volume (70 L), results in a half-life of $\ln 2 \cdot 70 / 5.6 \approx 9$ min. Thus, the 10% of the total cardiac output, 0.56 L/min, was considered as a reasonable cutoff value for drug classification in terms of CL_f since the half-lives of the highly cleared drugs range from 3.7 to 86.6 min for the physiological range of v_f values from 3 to 70 L, respectively; low cleared drugs ($CL_f < 0.56$ L/min) exhibit half-lives > 86.6 min irrespective of their v_f values. Accordingly, the cutoff points 63 L, 0.56 L/min in the v_f , CL_f plane is suggested for the classification of drugs into four categories, Fig. 3. Some drug examples classified according to PCS are presented in Table III. The PCS can be used complementary to the biopharmaceutics classification scheme (34) to formulate a global bio-

pharmaceutical-pharmacokinetic profile of drugs. This approach will certainly facilitate the pharmaceutical scientist to get an insight into bioavailability-disposition characteristics of a drug candidate in the early phases of development. However, further analysis will be required to elucidate the importance of the underlying physicochemical properties e.g., lipophilicity, solubility, plasma binding for the four drug categories of PCS.

Interspecies pharmacokinetic scaling primarily deals with clearance and volume of distribution; however, the combination of these approaches can be used for $t_{1/2}$ scaling (10). In the present study the allometric equations obtained for v_f and CL_f were used in conjunction with Eq. (5) to develop the corresponding allometric relationships for $t_{1/2}$. Figure 4 shows the frequency distribution of the exponent of the allometric equations (not reported) for $t_{1/2}$. The mean value of exponents was found 0.264, the median 0.258, while the $\pm 2SD$ interval lies between 0.219 and 0.308. Figure 4, demonstrates that the values of the exponent are normally distributed with a mean value very close to the theoretically expected value 0.25. Thus, the deviations of exponents of the allometric

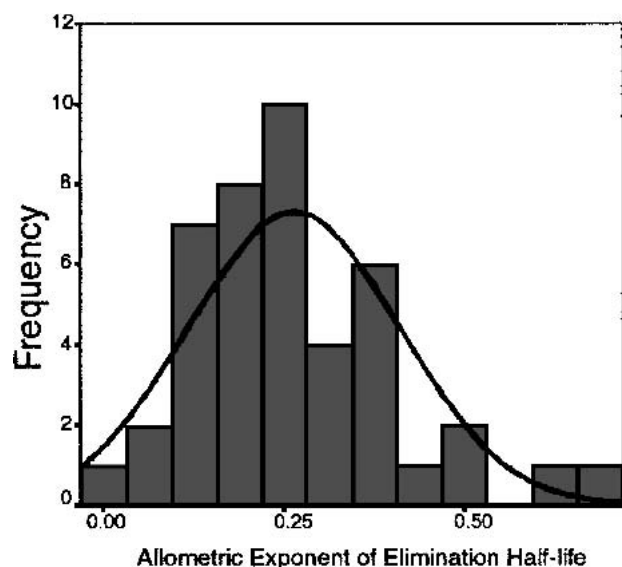
Table IV. Predicted and Observed Human Values of $t_{1/2}$

Drug	Predicted $t_{1/2}$ (h)		Observed $t_{1/2}$ ^a (h)
	Eq. 5 ^b	Eq. 2 ^c	
Actisomide	1.28	1.87	1.76
Amphotericin	38.23	65.64	68.67
Amsacrine	5.64	5.64	4.15
BSH	3.95	12.56	27.00
Cefazolin	1.23	2.38	1.41
Cefmetazole	0.59	0.60	0.89
Cefoperazone	1.75	1.75	1.57
Cefotetan	1.48	1.48	3.07
Cefpiramide	3.11	3.10	4.63
CI-921	2.67	2.67	1.38
Diazepam	3.99	3.97	12.97
Erythromycin	2.23	6.73	1.46
Moxalactame	1.68	1.69	1.20
Oleandomycin	2.07	2.15	0.98
Phencyclidine	5.47	9.54	14.61
Remoxipride	7.94	7.94	4.75
Theophylline	5.15	10.39	4.05
Statistical indexes			
AFRE	1.22	1.11	
%ARE	1.13	40.1	

^a Calculated from Eq. 2 using the reported V_{ap} and CL values.

^b Calculated from Eq. 5 using the predicted v_f and CL_f values.

^c Calculated from Eq. 2 using the predicted V_{ap} and CL_e values.

**Fig. 4.** Histogram for the allometric mass exponents of the elimination half-life, $t_{1/2}$.

equations of $t_{1/2}$ from 0.25 are most likely associated with the experimental errors encountered in the estimation of clearance and volume of distribution estimates across species.

Although the prediction of half-life from animals to humans is relatively difficult, many indirect methods have been suggested (10). In this study, the predicted values for v_f and CL_f were used to calculate the corresponding value of $t_{1/2}$ using Eq. (5). The results are presented in Table IV along with the predicted values for $t_{1/2}$ derived from Eq. (2) using CL_e and V_{ap} . The results of Table IV are controversial judging from the AFRE and %ARE values of the two approaches. However, the absolute values for the indexes AFRE and %ARE estimates were found 1.78 and 73.0% for $t_{1/2}$ calculated from Eq. (2) and 1.80 and 50.5% when $t_{1/2}$ was calculated from Eq. (5). This comparison indicates that predictions based on $t_{1/2}$ calculated from Eq. (5) seem to be more reliable.

CONCLUSIONS

The allometric relationships for v_f , CL_f rely exclusively on the physiologically sound, fractal consideration of drug distribution (3). The use of v_f values from animal species allows a reliable prediction of v_f in humans. Predictions for V_{ap} values based on v_f estimates are better than the current approaches. The mean values of the allometric exponents for CL_f and $t_{1/2}$ were found close to the theoretically expected values 0.75 and 0.25, respectively. Moreover, the values of these exponents for the data analyzed were homogeneously distributed around their means. Because the results for CL_f and $t_{1/2}$ are strongly linked to the estimates for v_f , it seems likely that the physiologically relevant v_f lends similar properties to CL_f and $t_{1/2}$. Thus, the predictive performance of CL_f was found better than other approaches which rely on various empirical assumptions, e.g., BW , MLP , rule of exponents. The predictive performance of the various clearance expressions for the conventional CL follows the ranking $(CL_f)_e > CL_e > CL_f$. The results for the prediction of $t_{1/2}$ seem to be more reliable when predictions are based on CL_f and v_f . Finally, a pharmacokinetic classification scheme was developed in the present study to be used as the basis for considering drug disposition phenomena.

REFERENCES

- J. G. Wagner. *Pharmacokinetics for the Pharmaceutical Scientist*, Technomic Publishing Company, Lancaster Pennsylvania, 1993.
- M. Rowland and T. Tozer. *Clinical Pharmacokinetics: Concepts and Applications*, Lea and Febiger, London, 1980.
- V. Karalis, L. Claret, A. Iliadis, and P. Macheras. Fractal volume of drug distribution: it scales proportionally to body mass. *Pharm. Res.* **18**:1056–1060 (2001).
- H. Boxenbaum and R. Ronfeld. Interspecies pharmacokinetic scaling and the Dedrick plots. *Am. J. Physiol.* **245**:R768–774 (1983).
- I. Mahmood and J. D. Balian. Interspecies scaling: Predicting pharmacokinetic parameters of antiepileptic drugs in humans from animals with special emphasis on clearance. *J. Pharm. Sci.* **85**:411–414 (1996).
- R. S. Obach, J. G. Baxter, T. E. Liston, B. M. Silber, C. Jones, F. Macintyre, D. J. Rance, and P. Wastall. The prediction of human pharmacokinetic parameters from preclinical and in vitro metabolism. *J. Pharmacol. Exp. Ther.* **283**:46–58 (1997).
- P. L. Bonate and D. Howard. Critique of prospective allometric scaling: Does the emperor have clothes? *J. Clin. Pharmacol.* **40**:335–340 (2000).
- P. L. Bonate and D. Howard. Rebuttal to Mahmood. *J. Clin. Pharmacol.* **40**:345–346 (2000).
- I. Mahmood. Prospective allometric scaling: Does the emperor have clothes? *J. Clin. Pharmacol.* **40**:341–344 (2000).
- I. Mahmood. Allometric issues in drug development. *J. Pharm. Sci.* **88**:1101–1106 (1999).
- B. Davies and T. Morris. Physiological parameters in laboratory animals and humans. *Pharm. Res.* **10**:1093–1095 (1993).
- I. Mahmood. Prediction of clearance, volume of distribution and half-life by allometric scaling and by use of plasma concentrations predicted from pharmacokinetic constants: a comparative study. *J. Pharm. Pharmacol.* **51**:905–910 (1999).
- C. Cook, L. Rozek, J. Stolzenbach, S. Anderson, G. Schoenhard, and A. Karim. Pharmacokinetics of a novel antiarrhythmic drug actinomide. *Pharm. Res.* **10**:427–433 (1993).
- A. Hutchaleelaha, H. H. Chow, and M. Mayersohn. Comparative pharmacokinetics and interspecies scaling of amphotericin B in several mammalian species. *J. Pharm. Pharmacol.* **49**:178–183 (1997).
- J. W. Paxton, S. N. Kim, and L. R. Whitfield. Pharmacokinetics and toxicity scaling of the antitumor agents amsacrine and CI-921, a new analogue, in mice, rats, rabbits, dogs and humans. *Cancer Res.* **50**:2692–2697 (1990).
- S. C. Mehta and R. D. Lu. Interspecies pharmacokinetic scaling of BSH in mice, rats, rabbits and humans. *Biopharm. Drug Dispos.* **16**:735–744 (1995).
- Y. Sawada, M. Hanano, Y. Sugiyama, and T. Iga. Prediction of the disposition of β -lactam antibiotics in humans from pharmacokinetic parameters in animals. *J. Pharmacokinetic. Biopharm.* **12**:241–261 (1984).
- M. Siefert, D. Maruhn, W. Maul, D. Forster, and W. Ritter. Pharmacokinetics of ciprofloxacin. *Arzneim.-Forsch./Drug Res.* **36**:1496–1502 (1986).
- U. Klotz, K. H. Antonin, and P. R. Bieck. Pharmacokinetics and plasma binding of diazepam in man, dog, rabbit, guinea pig and rat. *J. Pharmacol. Exp. Ther.* **199**:67–73 (1976).
- G. S. Duthu. Interspecies correlation of the pharmacokinetics of erythromycin, oleandomycin and tylosin. *J. Pharm. Sci.* **74**:943–946 (1984).
- T. Lavé, B. Levet-Trafit, A. H. Schmitt-Hoffmann, B. Morgenroth, W. Richter, and R. C. Chou. Interspecies scaling of interferon disposition and comparison of allometric scaling with concentration-time transformations. *J. Pharm. Sci.* **84**:1285–1290 (1995).
- T. Lavé, A. Saner, P. Coassolo, R. Brandt, A. H. Schmitt-Hoffmann, and R. C. Chou. Animal pharmacokinetics and interspecies scaling from animals to man of lamifiban, a new platelet aggregation inhibitor. *J. Pharm. Pharmacol.* **48**:573–577 (1996).
- M. S. Owens, W. C. Hardwick, and D. Blackall. Phencyclidine pharmacokinetic scaling among species. *J. Pharmacol. Exp. Ther.* **242**:96–101 (1987).
- M. Ishigami, K. Saburomaru, K. Niino, M. Kido, S. Morita, G. Miyamoto, and H. Kohri. Pharmacokinetics of procaterol in the rat, rabbit and beagle dog. *Arzneim.-Forsch./Drug Res.* **29**:266–270 (1979).
- M. Widman, B. Nilsson, B. Bryske, and J. Lundstrom. Disposition of remoxipride in different species, Species differences in metabolism. *Arzneim.-Forsch./Drug Res.* **43**:287–296 (1993).
- E. J. Hoogdalem, Y. Soeishi, H. Matsushima, and S. Higuchi. Disposition of the selective α_{1A} -adrenoceptor antagonist tamsulosin in humans: Comparison with data from interspecies scaling. *J. Pharm. Sci.* **86**:1156–1161 (1997).
- A. R. Gascon, B. Calvo, R. M. Hernandez, A. Dominguez-Gil, and J. L. Pedras. Interspecies scaling of cimetidine-theophylline pharmacokinetic interaction: Interspecies scaling in pharmacokinetic interactions. *Pharm. Res.* **11**:945–950 (1994).
- T. Izumi, S. Enomoto, K. Hosiyama, K. Sasahara, A. Shibukawa, T. Naragawa, and Y. Sugiyama. Prediction of the human pharmacokinetics of troglitazone, a new and extensively metabolized antidiabetic agent, after oral administration, with an animal scaled-up approach. *J. Pharmacol. Exp. Ther.* **277**:1630–1641 (1996).
- G. B. West, J. H. Brown, and B. J. Enquist. A general model for the origin of allometric scaling laws in biology. *Science* **276**:122–126 (1997).

30. G. B. West, J. H. Brown, and B. J. Enquist. The fourth dimension of life: Fractal geometry and allometric scaling of organisms. *Science* **284**:1677–1679 (1999).
31. I. Mahmood and J. D. Balian. Interspecies scaling: Predicting clearance of drugs in humans: three different approaches. *Xenobiotica* **26**:887–895 (1996).
32. J.G. Hardman, L.E. Limbird, P.B. Molinoff, R.W. Ruddon, and A.G. Gilman, *Goodman and Gilman's The pharmacological basis of therapeutics*, 9th ed, The McGraw-Hill companies, New York, 1996.
33. H. Boxenbaum. Time concepts in physics, biology, and pharmacokinetics. *J. Pharm. Sci.* **75**:1053–1062 (1986).
34. G. L. Amidon, H. Lennernas, V. P. Shah, and J. R. Crison. A theoretical basis for a biopharmaceutic drug classification: the correlation of in vitro drug product dissolution and in vivo bioavailability. *Pharm. Res.* **12**:413–420 (1995).